

1 Bayesian correlated models for assessing the
2 prevalence of viruses in organic and
3 non-organic agroecosystems

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5

6 **Abstract**

7

8 Virus diseases constitute one of the most important limiting factors in horticultural pro-
9 duction. Cultivation of horticultural species under organic management has increased in
10 importance in recent years. However, the sustainability of this new production method
11 needs to be supported by scientific research, especially in the field of virology. We
12 studied the prevalence of three important virus diseases in agroecosystems with regard
13 to its management system: organic *versus* non-organic, with and without greenhouse.
14 Prevalence was assessed by means of a Bayesian correlated binary model which con-
15 nects the risk of infection of each virus within the same plot and was defined in terms of
16 a logit generalized linear mixed model (GLMM). Model robustness was checked through
17 a sensitivity analysis based on different hyperprior scenarios. Inferential results were
18 examined in terms of changes in the marginal posterior distributions, both for fixed and
19 for random effects, through the Hellinger distance and a derived measure of sensitivity.
20 Statistical results suggested that organic systems show lower or similar prevalence than
21 non-organic ones in both single and multiple infections as well as the relevance of the
22 prior specification of the random effects in the inferential process.

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26 *ology.*

27 **1. Ordinary Text**

28 Society is becoming increasingly concerned about environmental damage caused by
29 agricultural activities. The sustainability of conventional agriculture is now being ques-
30 tioned, which is prompting traditional production systems to evolve toward production
31 methods that can protect both environmental and human health ([Van Bruggen, 1995](#);
32 [Bengtsson et al., 2005](#)).

33 In recent decades, organic agriculture has grown rapidly in comparison with other
34 agricultural systems. The adoption of these new agricultural practices has brought about
35 the need to compare low-input and conventional systems to verify whether agroecosys-
36 tem sustainability can be achieved ([Bettioli et al., 2004](#)). Despite the emergence of or-
37 ganic agriculture systems, the literature on their effects and interactions is scarce and
38 insufficient, above all in the field of virology ([Tomlinson, 1987](#)). Diseases caused by
39 viruses constitute a major threat to the large-scale production of crops worldwide, caus-
40 ing serious economic losses and undermining sustainability ([Gallitelli, 2000](#)). Assessing
41 the risk of infection should therefore be a priority in the study of the epidemiology of
42 such virus diseases.

43 The ecological and epidemiological factors that determine virus infections in veg-
44 etable crops are diverse and little is known about them. The sources and spread of
45 viruses, together with certain agricultural and horticultural practices, have a strong in-
46 fluence on their prevalence ([Hanssen et al., 2010](#)). In this respect, studies on the risk of
47 virus infections need to characterize the agroecosystem balance as well as understand
48 the complex relationships between organisms (plants, pathogens, and vectors) and envi-

49 ronment (Serra et al., 1999).

50 The main scientific question addressed in this paper is the study and comparison of
51 the risk of different virus infections in tomato and pepper plots characterized by their
52 agroecosystem. Specifically, we focus on the detection and quantification of the ef-
53 fects associated with organic management. The agroecosystem of each plot is defined
54 through a set of covariates containing information on its management conditions and al-
55 titude. Agroecosystems are dynamic entities (Finley et al., 2011) with complex sources
56 of uncertainty and hierarchies. Following Thornley and France (2007), the estimation of
57 the infection risk of different viruses within the same plot would require the modelling
58 of not only a suitable set of covariates but also the inclusion of some probabilistic terms
59 which connect the different observations of the same individual.

60 The inclusion of dependence and/or correlation relationships among variables, re-
61 sponse and/or covariates, is usually done by means of random effects whose stochastic
62 nature adds much more probability to the structure of the model. Bayesian reasoning
63 provides a natural environment for analysing them mainly because of the own concep-
64 tion of the Bayesian probability theory, which specifies all the uncertainties in the model
65 through probabilistic elements (Loredo, 1990). Some applied papers that illustrate the
66 benefits of hierarchical Bayesian models in biometrics scenarios are Alvares et al. (2016)
67 in agriculture, Paradinas et al. (2015) in fisheries, Paciorek et al. (2009) in forestry, and
68 Clark et al. (2007) in ecology.

69 A Bayesian binary correlated model under the generalized linear mixed models
70 (GLMM) specification was considered to perform a regression analysis of the prevalence
71 of the different viruses. Random effects were used to correlate the risk of infection of
72 each virus in the same plot and quantify the intra-plot ability to be infected. Robustness
73 in hierarchical Bayesian models is a major concern as it can be affected by an inappro-
74 priate choice of the hyperprior distributions for hyperparameters (Lambert et al., 2005;

75 Gelman, 2006; Roos and Held, 2011; Roos et al., 2015). To this effect, the sensitivity
76 of the modelling was tested using several specifications for the hyperprior distribution
77 of the random effects scale parameter. A general measure based on the Hellinger dis-
78 tance (Le Cam, 2012), with its calibration, was used to quantify discrepancies in the
79 subsequent posterior marginal distribution of the common regression coefficients and
80 hyperparameter.

81 The remainder of this article is organized as follows: Section 2 reviews the data and
82 presents the formulation of the model. Section 3 reports and discusses the results with
83 regard to multiple and single viral infections. Section 4 proposes several random effects
84 specifications and analyses the robustness of the estimated models through a sensitivity
85 measure based on the Hellinger distance. Some concluding remarks are given in Section
86 5.

87 **2. Viruses data and statistical modelling**

88 **2.1. Data description**

89 Globally, about 30 viruses are capable of affecting the most known horticultural crops.
90 However, despite being able to infect a wide variety of species, they usually affect
91 Solanaceae species, specially tomato (*Solanum lycopersicum*) and pepper (*Capsicum*
92 *annuum L.*). These species are two of the most common vegetable crops grown in Spain
93 whose production is being seriously limited by virus diseases. There has recently been a
94 considerable increase in the cultivation of these vegetables under integrated systems such
95 as organic agriculture. It is therefore essential to carry out subsequent virus prevalence
96 studies in order to guarantee their sustainability.

97 A project under the auspices of the Valencian Institute Agricultural Research was
98 conducted in the summer of 2012 in the Valencian region for this purpose. A total of
99 30 plots in tomato and pepper production were selected according to their system of
100 production. Each plot was evaluated in terms of its agroecosystem characterization and

101 the presence or absence of three different viral infections in the crops: tomato mosaic
102 virus (ToMV), cucumber mosaic virus (CMV) and tomato spotted wilt virus (TSWV).
103 These viruses affect both tomato and pepper crops equally, are transmitted in different
104 ways, and can cause substantial economic losses. The presence of each specific virus
105 infection in a plot was assumed when the virus was detected in at least one of eight
106 randomly-selected plants. The enzyme-linked immunosorbent assay (ELISA) technique
107 (Clark et al., 1976) was used to detect each virus.

108 The assessment of the agroecosystem of each plot was determined by its manage-
109 ment condition and altitude. Management condition was evaluated by classifying each
110 plot as organic, non-organic with greenhouse structure, and non-organic with no green-
111 house structure. These categories were defined according to the most representative
112 agroecosystems in Spanish agriculture. Organic plots differ from the non-organic ones
113 in many respects, but substantial differences are related to the use of agrochemicals
114 and other external inputs with important influence in pest and disease prevalence. In
115 fact, some purported drawbacks related to organic agriculture include an increasing in-
116 cidence of pest damage and higher risks of pest outbreaks (Letorneau and Goldstein,
117 2001). All plots classified as organic complied with the current regulation and were
118 certificated as such by the Organic Agriculture Committee of the Autonomous Govern-
119 ment of València. The presence of greenhouse in non organic plots was also considered
120 because is a frequent practice in non-organic systems. The use of covering protections
121 suppose a physical barrier which is directly related to virus infection in the sense that
122 denies insects (vector of virus transmission) acces to plants.

123 Of the total of 30 plots of our study, 18 were classified as organic and 12 as non-
124 organic, 5 of them with greenhouse structure. For organic plots, the proportion of in-
125 fected plants with ToMV, CMV, and TSWV was 0.222, 0.167, and 0.056, respectively.
126 In the case of non-organic plots with greenhouse these proportions were 0.400, 0.200,

127 and 0.200, respectively, and 0.143, 0.286, and 0.286 for non-organic plots without green-
 128 house. The organic plots presented a lower proportion of plants infected by CMV and
 129 TSWV viruses, but the prevalence of ToMV was lowest in the non-organic plots with no
 130 greenhouse.

131 **2.2. Statistical model**

132 We consider a logit GLMM for correlated binary responses (Ntzoufras, 2009) to model
 133 the Bernoulli random variable Y_{ij} which describes the presence or absence of virus j
 134 ($j = 1$ corresponds to ToMV, $j = 2$ to CMV, and $j = 3$ to TSWV) in plot i ,

$$(Y_{ij} | \theta_{ij}) \sim \text{Bernoulli}(\theta_{ij}), \quad (1)$$

$$\text{logit}(\theta_{ij}) = \mathbf{x}_i^\top \boldsymbol{\beta}_j + b_i, \quad i = 1, \dots, 30,$$

135 where θ_{ij} is the probability that virus j will be detected in plot i and represents risk of
 136 infection; \mathbf{x}_i is the vector of covariates; $\boldsymbol{\beta}_j$ is the corresponding vector of the regression
 137 coefficients; and $(b_i | \sigma_b^2) \sim \text{N}(0, \sigma_b^2)$ is a normal random effect associated with plot
 138 i with mean zero and standard deviation σ_b . The three management conditions were
 139 coded in a sequence of two dummy variables (organic and non-organic, with and without
 140 greenhouse structure) to avoid overparameterization, with organic management as the
 141 reference category.

142 Random effects capture within-plot variability and correlate prevalence among all
 143 viruses so that each individual virus infection is determined by its own agroecosystem
 144 effect and an individual effect plot which denotes its ability to be infected. They also
 145 provided conditional independence among the prevalence of the three viruses as follows

$$P(Y_{ij} = y_j, j = 1, 2, 3 | \boldsymbol{\beta}, b_i, \mathbf{x}_i) = \prod_{j=1}^3 P(Y_{ij} = y_j | \boldsymbol{\beta}_j, b_i, \mathbf{x}_i), \quad (2)$$

146 where $y_j \in \{0, 1\}$, $j = 1, 2, 3$, $\boldsymbol{\beta} = (\boldsymbol{\beta}_1, \boldsymbol{\beta}_2, \boldsymbol{\beta}_3)^\top$, and the conditional probability that plot

147 i will be infected with virus j can be expressed as

$$P(Y_{ij} = 1 \mid \boldsymbol{\beta}_j, b_i, \mathbf{x}_i) = \frac{\exp\{\mathbf{x}_i^\top \boldsymbol{\beta}_j + b_i\}}{1 + \exp\{\mathbf{x}_i^\top \boldsymbol{\beta}_j + b_i\}}, \quad (3)$$

148 The joint marginal distribution obtained integrating out the random effects in (4),

$$P(Y_{ij} = y_j, j = 1, 2, 3 \mid \boldsymbol{\beta}, \sigma_b, \mathbf{x}_i) = \int P(Y_{ij} = y_j, j = 1, 2, 3 \mid \boldsymbol{\beta}, b_i, \mathbf{x}_i) \mathcal{N}(b_i \mid 0, \sigma_b) db_i, \quad (4)$$

149 does not depend on the subject-specific random effects and can be interpreted as the com-
150 mon risk infection of a generic plot from the population with the same agroecosystem
151 and altitude.

Inference was carried out using Bayesian statistics. We therefore needed to elicit a prior distribution for the parameters and hyperparameters to complete the Bayesian model. We considered a prior independent default scenario with normal distributions centered at zero and a wide variance for the regression coefficients. As previously introduced, the specification of a hyperprior distribution for the random effects scale parameter is a challenging issue (Lambert et al., 2005; Gelman, 2006; Roos and Held, 2011; Roos et al., 2015). Section 4 contains a sensitivity analysis of the performance of various traditional hyperprior choices (gamma, uniform and half-normal) in our study. This analysis led us to choose the uniform distribution $\text{Un}(\sigma_b \mid 0, 100)$ for the standard deviation of the random effects. Consequently

$$\begin{aligned} \pi(\boldsymbol{\beta}, \sigma_b) &= \prod_{j=1}^3 \prod_{k=0}^3 \pi(\beta_{jk}) \pi(\sigma_b) \\ &= \prod_{j=1}^3 \prod_{k=0}^3 \mathcal{N}(\beta_{jk} \mid 0, \sigma^2 = 1000) \text{Un}(\sigma_b \mid 0, 100) \end{aligned} \quad (5)$$

152 where $\boldsymbol{\beta}_j = (\beta_{j0}, \beta_{j1}, \beta_{j2}, \beta_{j3})^\top$ are the regression coefficients associated with organic,
153 non-organic with and without greenhouse and altitude (in logarithmic scale) for virus j .

154 **3. Results**

155 The posterior distribution $\pi(\boldsymbol{\beta}, \sigma_b | \mathcal{D})$, where \mathcal{D} denotes data, was approximated using
156 Markov chain Monte Carlo (MCMC) simulation methods with WinBUGS Software
157 (Lunn et al., 2000). Random effects models, and Bayesian categorical GLMs in particular,
158 involve many computational difficulties (Albert and Chib, 1993). We fixed the
159 number of iterations and the burn-in period with very large values to avoid strong correlation
160 in the MCMCs samples and get a reliable sample of the posterior distribution.
161 Specifically, simulation was run considering three Markov chains with 1 000 000 iterations
162 and a burn-in period with 100 000. In addition, the chains were thinned by storing
163 every 10th iteration in order to reduce autocorrelation in the saved sample and avoid
164 computer memory problems.

165 Trace plots of the simulated values of the chains appear overlapping one another,
166 indicating stabilization. Convergence of the chains to the posterior distribution was assessed
167 using the potential scale reduction factor, \hat{R} , and the effective number of independent
168 simulation draws, neff . In all cases, the \hat{R} values were equal or close to 1 and neff
169 > 100 , thus indicating that the distribution of the simulated values between and within
170 the three chains was practically identical, and that sufficient MCMC samples had been
171 obtained, respectively (Gelman and Rubin, 1992).

172 **3.1. Management conditions**

173 Multiple viral infections that may result in synergisms or antagonisms are frequently
174 found in nature, with unpredictable pathological consequences. Synergistic interactions
175 resulting from mixed infections with two or more viruses are common and well documented
176 in plants (García-Cano et al., 2006). Viral synergism could affect various growth
177 variables such as plant height, weight, and yield (Murphy and Bowen, 2006), and in extreme
178 cases can lead to plant death.

179 The joint posterior distribution, $\pi(P(Y_{ij} = y_j, j = 1, 2, 3 \mid \boldsymbol{\beta}, \boldsymbol{\sigma}_b, \boldsymbol{x}_i) \mid \mathcal{D})$, where $y_j \in$
180 $\{0, 1\}$, of the risk infection given in (4) for a generic plot at given altitude in each of the
181 management systems is the basic tool for assessing such synergisms and antagonisms.
182 This posterior distribution is also the starting point for the computation of relevant con-
183 ditional or marginal inferences.

184 We begin by discussing some results about multiple viral infections with regard to
185 plot management condition: the posterior distribution of the prevalence of the total num-
186 ber of viruses in a plot and the posterior distribution of the risk of a third infection in
187 plots already infected with two of the viruses. Figure 1a shows the mean of the posterior
188 distribution associated to the presence of 0, 1, 2 and 3 viruses in a generic plot i located
189 at 76 meters of altitude (the sample mean) with regard to its management system. Most
190 of the plots have no infections, but the organic ones present the highest rates for plots
191 without infections. Non-organic plots, with and without greenhouse, behave similarly.

192 Figure 1b shows the posterior mean of the risk of a third infection in plots already
193 infected with two of the viruses. Outcomes are also obtained for a generic plot i situ-
194 ated at 76 meters of altitude (the sample mean) with regard to its management system.
195 For condition ToMV in the presence of CMV and TSWV, organic and non-organic with
196 greenhouse plots behave similarly with probabilities around 0.6. This is not the case
197 for non-organic with no greenhouse plots, with an estimated probability close to 0.2.
198 CMV infection given ToMV and TSWV presents homogeneous results in all manage-
199 ment systems, with a higher difference among estimated probabilities of 0.167. The
200 pattern for the probability of a TSWV infection in plots already infected with ToMV
201 and CMV seems to be different among the management conditions: non-organic with
202 no greenhouse systems shows the highest probability (0.514), followed by non-organic
203 with greenhouse plots (0.316), and organic (0.172), respectively. It is difficult to detect
204 a general trend on conditional infections among the different agroecosystems analysed.

205 This is a very interesting subject and surely a new study with more data would be nec-
 206 essary in order to better understand them.

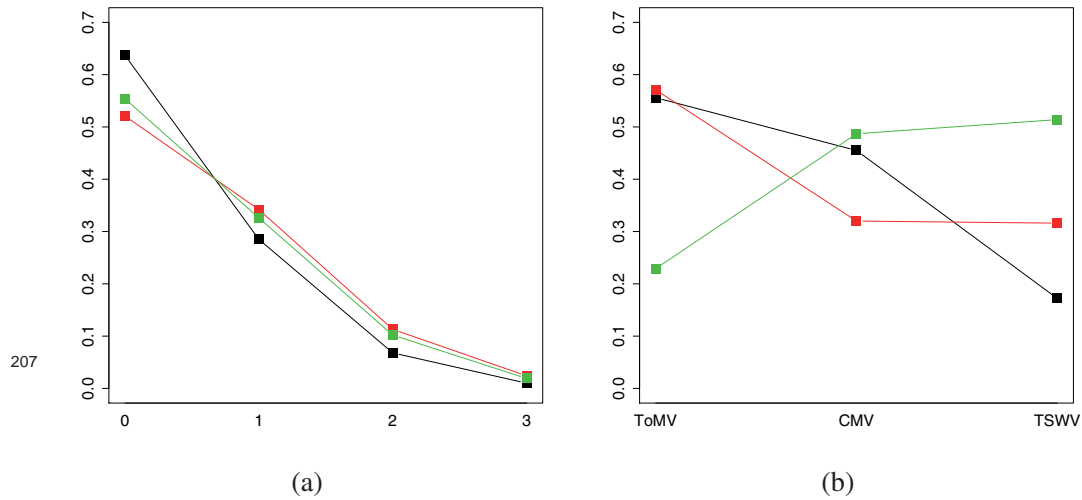


Figure 1: (a) Probability (mean of the posterior distribution) for the presence of 0, 1, 2 and 3 viruses in organic (black), non organic-green (red) and non organic-non green (green) management systems. (b) Probability (mean of the posterior distribution) of the risk of a third infection in plots already infected with two of the viruses in organic (black), non organic-green (red) and non organic-non green (green) management systems.

208 The marginal effect of the management conditions in each virus was assessed through
 209 the marginal posterior distribution $\pi(P(Y_{ij} = 1 | \boldsymbol{\beta}, \boldsymbol{\sigma}_b, \mathbf{x}_i) | \mathcal{D})$. Table 1 shows a descrip-
 210 tive of the posterior distribution of the risk of infection for each virus and management
 211 conditions for a generic plot situated at a height of 76 meters (the sample median). The
 212 lowest risk of infection for a generic plot under organic management is for TSWV virus.
 213 The most relevant differences among the management conditions were found for virus
 214 ToMV. In contrast, virus CMV seemed the most stable. However, the organic effect was
 215 weaker for ToMV risk, approximately about four times the one for TSWV virus. It is
 216 important to mention the great uncertainty associated to all marginal posterior distribu-
 217 tions in the analysis, mainly due to the combination of the reduced size of the sample and
 218 the usual scarce information of binary data. To this effect, a bigger experiment would be
 219 necessary for a more informative and objective study that allows to reach more precise

220 conclusions about the subject.

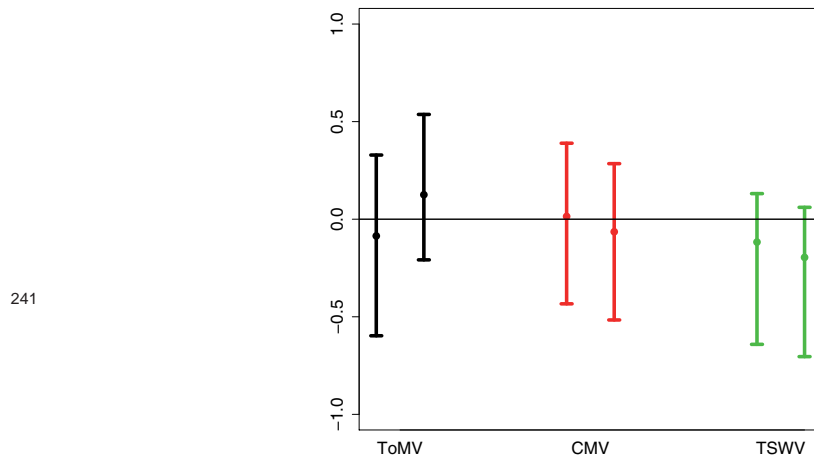
221 **Table 1:** Summary of the posterior distribution of the risk of infection for each management condition and virus.

Virus	Management	Mean	Sd	$Q_{2.5\%}$	$Q_{50\%}$	$Q_{97.5\%}$
ToMV	Organic	0.225	0.184	0.008	0.181	0.734
	Non-organic, greenhouse	0.311	0.252	0.006	0.248	0.900
	Non-organic, no greenhouse	0.100	0.147	0.000	0.041	0.553
CMV	Organic	0.169	0.161	0.004	0.124	0.634
	Non-organic, greenhouse	0.155	0.190	0.001	0.080	0.719
	Non-organic, no greenhouse	0.234	0.216	0.004	0.168	0.809
TSWV	Organic	0.057	0.093	0.000	0.026	0.309
	Non-organic, greenhouse	0.174	0.203	0.001	0.095	0.764
	Non organic, no greenhouse	0.253	0.223	0.005	0.189	0.831

223 Comparison of the three management systems was also quantified with the posterior
 224 distribution of the risk difference (RD) (Christensen et al., 2011). RD is an absolute and
 225 intuitive measure of association for quantifying difference between proportions associ-
 226 ated to an outcome of interest in two groups. It is defined in $[-1, 1]$ so that $RD = 0$
 227 means no difference between groups, $-1 \leq RD < 0$ that risk is greater in group 2, and
 228 $0 < RD \leq 1$ the opposite.

229 Figure 2 shows, for each virus, the posterior mean and 95% credible interval of the
 230 RD between organic and non-organic, with and without greenhouse, generic plots. Infor-
 231 mation provided by this graphic reaffirms the results in Table 1. Note that the differences
 232 between organic management conditions and the two non-organic conditions are clear in
 233 the case of TSWV infection: both posterior distributions are highly concentrated on the
 234 negative RD values with associated posterior probabilities 0.764 and 0.910 when com-
 235 paring organic and non-organic with and without greenhouse management, respectively.
 236 For CMV infections, the results are less clear, with posterior probabilities of 0.395 and
 237 0.611, respectively. In the case of ToMV infection, there are few differences between

238 organic and non-organic with greenhouse conditions (posterior probability of a negative
 239 difference is 0.620), but a relevant probability, 0.84, that the risk of infection will be
 240 greater in organic than in non-organic without greenhouse.



241

Figure 2: Posterior mean and 95% credible interval of the *RD* between organic system in relation to non organic-green (left) and non organic-no green (right) system for ToMV, CMV and TSWV infections.

242 3.2. Altitude condition effect

243 Plot altitude is a relevant epidemiological information due to its important role in shap-
 244 ing insect vector distributions and virus survival. The effect of altitude on the risk of
 245 infection is clearly negative in all viruses and therefore we can expect a decrease of the
 246 risk of infection as altitude increases. Figure 3a shows the posterior distribution of the
 247 regression coefficient associated to altitude for each virus: -0.914 , -0.745 and -0.480
 248 are, respectively, the subsequent posterior mean of the coefficient for virus ToMV, CMV,
 249 and TSWV, with posterior probabilities 0.940, 0.904, and 0.768 associated to their neg-
 250 ative values. Note that virus ToMV is the most negatively associated with altitude. Fig-
 251 ure 3b shows the posterior distribution of the *RD* between two generic organic plots with
 252 altitudes of 16 and 604 m, the lowest and highest values of the organic plots in the sam-
 253 ple. These graphics are in line with the previous comments and also indicate the less

254 important role of altitude in the risk of a TSWV infection in organic crops.

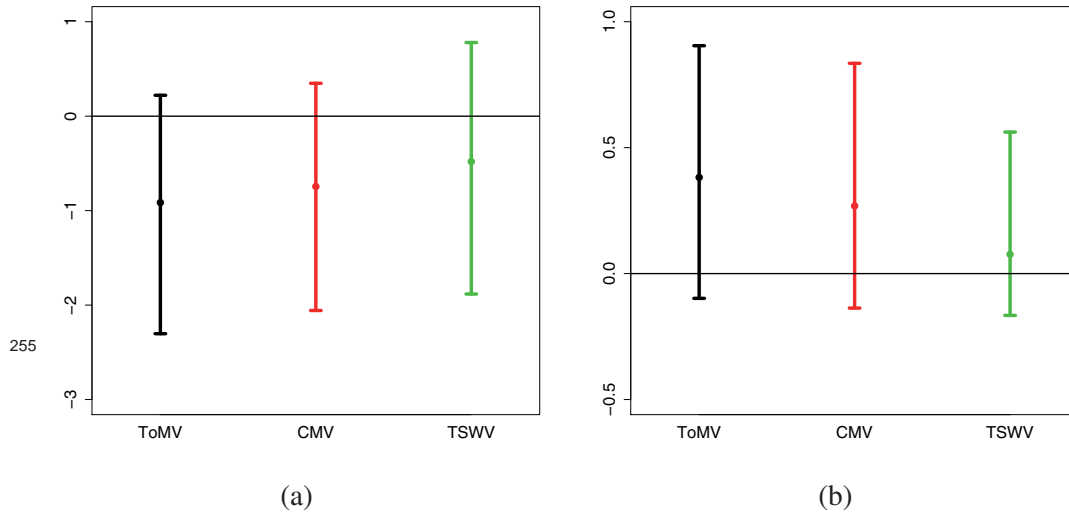


Figure 3: For virus ToMV (in black), CMV (in red), and TSWV (in green): posterior mean and 95% credible interval of the regression coefficient associated to the altitude (in logarithmic scale) (a), and posterior distribution of the RD between a typical organic plot at altitudes 16 and 604 m (b).

256 3.3. Individual random effects

257 Random effects for each plot capture the ability to be infected of individual plots, thus
 258 correlating the risk of infection among the viruses of each plot. Since each individual
 259 random effect is responsible for the differences in the estimation of the risk between
 260 plots managed under similar agroecosystem conditions, quantifying their contribution to
 261 the analysis in terms of factors and covariates is highly relevant to our understanding of
 262 the weight of the common and individual elements in the model.

263 The mean of the posterior distribution of the standard deviation, σ_b , of the plot ran-
 264 dom effect is 0.968 with a 95% credible interval [0.046, 2.671]. In addition, we assessed
 265 the contribution of the random effect associated to each plot towards the conditional
 266 posterior distribution of the risk of infection $\pi(P(Y_{ij} = 1 | \boldsymbol{\beta}, b_i, \mathbf{x}_i) | \mathcal{D})$. It was esti-
 267 mated individually for the three viruses at the altitude of 76 meters with the purpose of

268 assessing differences in risk infection among individuals that share the specification of
269 the vector of covariates \mathbf{x}_i , that is to say, plots that were managed under the same system.
270 Figure 4 shows a mosaic of subfigures in which each one displays the posterior expect-
271 ation of the risk of infection for each plot grouped according to management condition
272 (rows) and the type of virus infection (columns).

273 We can distinguish a certain stability in risk infection regarding individuals belong-
274 ing to non-organic no greenhouse systems (row 3) with maximum differences among
275 individuals of 0.039, 0.084 and 0.090 for ToMV, CMV and TSWV respectively. Non-
276 organic with greenhouse plots (row 2) are less similar with maximum differences in risk
277 infection no greater than 0.190 (ToMV). Organic plots showed the most remarkable dif-
278 ferences among their individuals, with maximum differences of 0.211 for ToMV and
279 0.231 for CMV. In contrast TSWV showed the opposite behaviour with a slight maxi-
280 mum difference of 0.087. In conclusion, we suspect the strong relevance of the common
281 elements in the model (fixed effects) in the case of non-organic and no greenhouse plots
282 regardless of virus infection. On the other hand, in the case of organic plots the weight
283 of the common elements effect in the model was not so evident considering that not all
284 viruses exhibited a similar tendency: ToMV and CMV risk infection varied considerably
285 among individuals, but this was not the case with TSWV.

286 4. Sensitivity analysis

287 Bayesian GLMMs are a particular class of models for which the estimation process can
288 be seriously affected by the elicitation of prior distributions for the random effects scale
289 parameter (standard deviation, σ_b , or a one-to-one transformation of it, variance σ_b^2 or
290 precision $\tau_b = 1/\sigma_b^2$). Special attention is required in studies where the number of groups
291 is small, σ_b is close to zero, and/or the number of groups is large compared to the num-
292 ber of observations in each group (Box and Tiao, 1992; Gelman, 2006; Roos and Held,

293 2011). This latter situation is the case of our study, with $I = 30$ plots and only three
294 observations in each of them. An additional element that aggravates the situation is the
295 sparsity of the data due to its categorical, binary condition. We conducted a sensitivity
296 analysis of the posterior distribution to the specification of several prior hyperdistribu-
297 tions for the random effects scale parameter. This analysis was based on the methodol-
298 ogy developed in McCulloch (1989), Roos and Held (2011), and Roos et al. (2015) re-
299 garding the stability of the marginal posterior distribution of the regression coefficients
300 of the model and the relative changes in the subsequent marginal posterior distributions
301 of the random effects scale parameter.

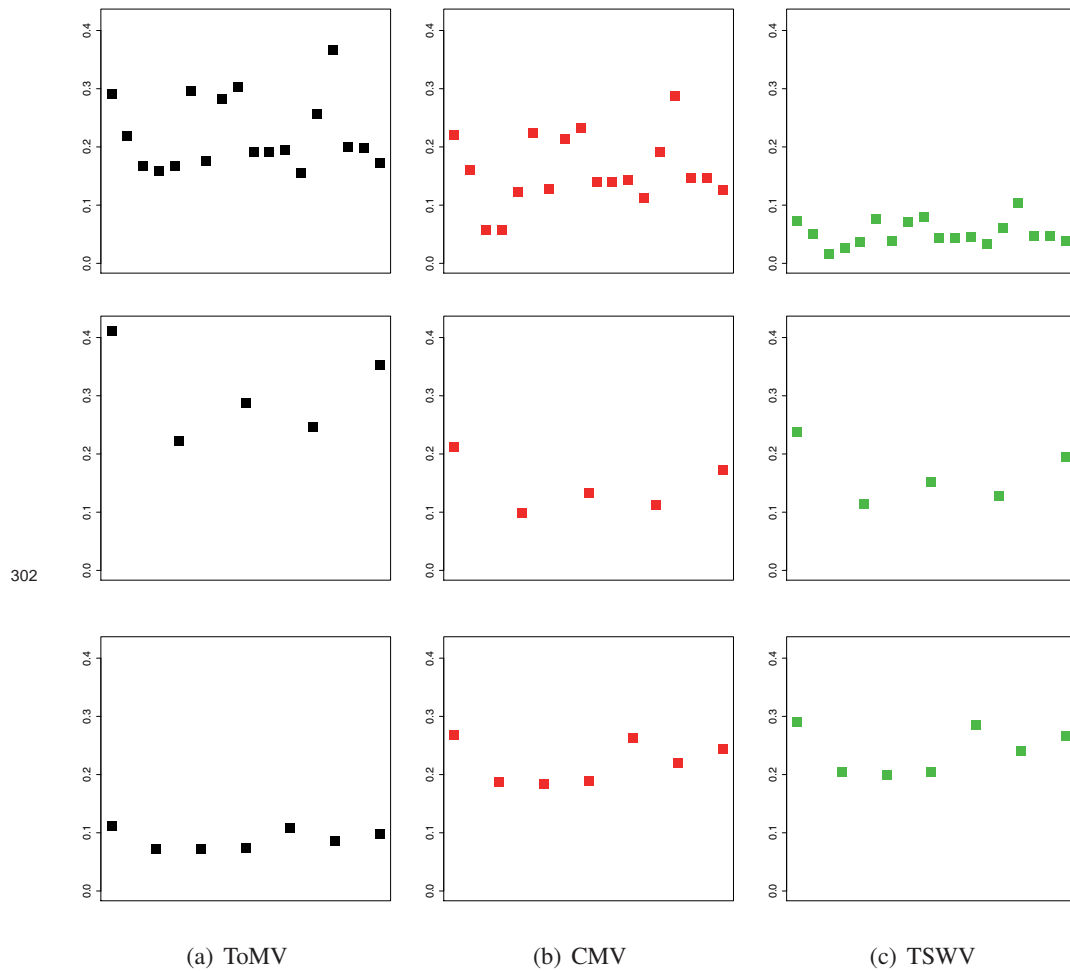


Figure 4: Posterior mean of the conditional posterior distributions associated to management systems organic (row 1), non organic and greenhouse (row 2) and non organic and non greenhouse (row 3) for viruses ToMV (column1), CMV (column 2) and TSWV (column 3) obtained from a fixed altitude value of 76 m.

303 **4.1. Hyperprior distributions**

304 For the random effects scale parameter, different hyperprior distributions were specified

305 for τ_b within the family of gamma, and for σ_b within uniform and half-normal distribu-

306 tions

- 307 • Gamma: $Ga(0.001, 0.001)$, $Ga(0.005, 0.005)$, and $Ga(0.05, 0.05)$ (Ga_1 , Ga_2 , and
308 Ga_3 , respectively),
- 309 • Uniform: $Un(0, 100)$, $Un(0, 55.63)$, and $Un(0, 7.92)$ (Un_1 , Un_2 , and Un_3), and
- 310 • Half-normal: $HN(10)$, $HN(3.0387)$, and $HN(0.3965)$ (HN_1 , HN_2 , and HN_3).

311 Gamma distributions were parameterized in terms of a shape and a rate parameter,
312 and half-normal distributions were set according its standard deviation. Hyperdistribu-
313 tions Ga_1 , Un_1 , and HN_1 were considered the default choices due to their “noninfor-
314 mative” nature and their common use in Bayesian applications. In addition, two other
315 hyperparameter specifications within each family of hyperdistributions were contem-
316 plated to assess the effect of small and medium perturbations in the hyperparameter
317 specifications on posterior inferences. These hyperprior distributions were set following
318 the criterion of the Hellinger distance (Le Cam, 2012). This is a symmetric and invari-
319 ant measure of discrepancy between two probability distributions taking values between
320 0 and 1, where the value 0 represents no divergence and 1, full divergence (See Ap-
321 pendix 1).

322 Hyperparameter values were assessed considering two reference Hellinger distance
323 values, a small and a medium perturbation. This computation was based on the analytical
324 expression of the Hellinger distance between gamma, uniform and half-normal distribu-
325 tions (see Appendix 1). Small perturbation was associated to a Hellinger distance of
326 0.541 and medium to 0.848. Consequently, Ga_2 , Un_2 , and HN_2 hyperparameteres were
327 determined to obtain a Hellinger distance of 0.541 in relation to hyperdistributions Ga_1 ,
328 Un_1 , and HN_1 , respectively. Hyperparameter values for Ga_3 , Un_3 , and HN_3 were se-
329 lected because of their Hellinger distance, 0.848, to hyperpriors Ga_1 , Un_1 , and HN_1 ,
330 respectively.

331 Focusing on gamma hyperdistributions, Ga1 exhibits the widest range of uncertainty
332 with a variance of 1000. It is frequently used in many of the examples provided with the
333 WinBUGS software (Lunn et al., 2012) and shows a uniform shape for most of the range
334 with a spike of probability density near zero. Ga2 and Ga3 share this shape, although
335 they show lower range coverage as a consequence of their fewer variance values, 200
336 and 20. Hyperprior Un1 is recommended by Spiegelhalter et al. (2004) in their book on
337 clinical trials. It is a very generous distribution allowing for a great space of values due
338 to its variance of 833.3. Un2 and Un3 display variance values of 257.84 and 5.23, and
339 as such they are very different from the non-null density range. The half-normal default
340 option, HN1, is a choice used in Thompson et al. (1997) and Roos and Held (2011). It
341 exhibits a variance of 36.3 giving a low probability to values greater than this. HN2 and
342 HN3 are more informative versions, especially HN3 with a variance value of 0.06.

343 We conducted nine independent inferential processes with the same data and the
344 same marginal prior distribution $\pi(\boldsymbol{\beta})$ for the regression coefficients as in (5) but varying
345 marginal hyperprior distribution according to the specifications previously presented.

346 **4.2. Sensitivity of the regression coefficients**

347 We discuss sensitivity of the marginal posterior distributions of the regression coeffi-
348 cients derived from the inferential processes described above. Discrepancies among the
349 estimates of posterior marginal distributions were the result of alterations in the hyper-
350 prior values. Hellinger distances between posterior marginal distributions approximated
351 by MCMC methods were computed via expression (A.1) in Appendix 1 and imple-
352 mented by means of the function `HDistNoSize` in the R package `bmK` (Krachey and Boone,
353 2012). Furthermore, to facilitate interpretation these values were calibrated with regard
354 to a normal distribution with variance 1 (see Appendix 2 for more details about calibra-
355 tion).

356 Table 2 shows the calibration of the Hellinger distance between the posterior marginal

357 distribution of the different coefficients of regression computed from the hyperpriors
358 considered. In none of the comparisons the discrepancies observed were greater than the
359 differences between the normal distributions $N(0, 1)$ and $N(0.284, 1)$, which reveals that
360 Hellinger values are in general close to zero (see Table 4 in Appendix 2 where a calibra-
361 tion of the normal mean related to its subsequent Hellinger distance is displayed). Uni-
362 form distributions have the smallest discrepancies despite the existing differences among
363 hyperpriors Un1, Un2, and Un3. The behaviour of half-normal distributions was similar
364 to that of the uniform distributions in the case of hyperpriors HN1 and HN2. Neverthe-
365 less, inference from hyperprior HN3 exhibited the greatest discrepancies, surely due to
366 its informative nature. Gamma showed greater discrepancies than uniform hyperpriors
367 in all cases, although in none of the scenarios did these differences exceed those ob-
368 tained from hyperprior HN3. Thus, the above comments enable us to conclude that our
369 assumptions on the choice of hyperparameter prior distribution influences the estimates
370 of the regression coefficients only to a minor extent.

371 We now discuss the effect of the different hyperpriors considered on the posterior
372 distribution of each regression coefficient. Figure (5) is a mosaic of subfigures. Each
373 subfigure displays the posterior mean of the regression coefficients of the different infer-
374 ential processes conducted. The order of the points corresponds to the order in which hy-
375 perpriors are presented (Ga1, Ga2, Ga3; Un1, Un2, Un3; and HN1, HN2, HN3). A great
376 similarity can repeatedly be seen, in practically all coefficients and viruses, between re-
377 sults from hyperpriors HN1 and HN2, and also those from the uniform hyperpriors. As
378 expected, results from HN3 are very different, most likely due to its informative char-
379 acteristics. Finally, posterior means from the analyses based on the gamma hyperpriors
380 vary the most, indicating a greater sensitivity to parameter specification.

Table 2: Calibration of the Hellinger distance between the posterior marginal distribution of the coefficients of regression associated to organic (β_o), non-organic with greenhouse (β_{no-g}), non-organic without greenhouse (β_{no-ng}) and altitude in logarithmic scale (β_{alt}) computed from hyperprior distributions Ga1 and Ga2, Ga1 and Ga3, Un1 and Un2, Un1 and Un3, HN1 and HN2, and HN1 and HN3.

Virus	Coeff.	(Ga1,Ga2)	(Ga1,Ga3)	(Un1,Un2)	(Un1,Un3)	(HN1,HN2)	(HN1,HN3)
ToMV	β_o	0.038	0.084	0.024	0.022	0.034	0.236
	β_{no-g}	0.032	0.068	0.019	0.019	0.035	0.197
	β_{no-ng}	0.020	0.042	0.018	0.020	0.024	0.124
	β_{alt}	0.043	0.099	0.022	0.024	0.039	0.284
CMV	β_o	0.033	0.068	0.023	0.021	0.034	0.201
	β_{no-g}	0.029	0.056	0.021	0.019	0.025	0.148
	β_{no-ng}	0.029	0.060	0.019	0.020	0.027	0.171
	β_{alt}	0.037	0.085	0.023	0.023	0.038	0.249
TSWV	β_o	0.022	0.052	0.019	0.021	0.030	0.144
	β_{no-g}	0.024	0.043	0.021	0.020	0.025	0.108
	β_{no-ng}	0.023	0.048	0.020	0.019	0.025	0.139
	β_{alt}	0.028	0.069	0.020	0.019	0.034	0.193

4.3. Sensitivity of the variability of the random effects

We now discuss and assess the sensitivity of the random effects scale parameter corresponding to the inferential processes described in Subsection 4.1. Figure 6 shows the posterior marginal distribution (mean and 95% credible intervals) of the standard deviation of the random effects. It is worth noting that in the case of the gamma hyperpriors, the posterior marginal distribution $\pi(\sigma_b | \mathcal{D})$ is computed from the joint posterior $\pi(\boldsymbol{\beta}, \tau_b | \mathcal{D})$, which is based on the prior $\pi(\boldsymbol{\beta}, \tau_b)$. The results from the uniform hyperdistribution are stable, since the subsequent marginal posterior distributions are virtually indistinguishable. The opposite occurs for results from the gamma hyperpriors, with very different posterior distributions greatly influenced by the spike near zero of the subsequent hyperprior. The half-normal distribution also exhibits a sensitive performance, with the posterior distributions from HN1 and HN2 practically equal to those from the

395 uniform distribution. As previously noted, the exception is for the posterior distribution
396 from the informative HN3.

Finally, we used a sensitivity measure developed in [Roos and Held \(2011\)](#) to evaluate the relative change in the posterior marginal distribution of the random effects scale parameter with regard to subsequent change in the prior distribution. Changes in both prior and posterior distributions are assessed through the ratio between two Hellinger metrics in the form

$$S(\pi_1, \pi_2) = \frac{H(\pi_1(\theta | \mathcal{D}), \pi_2(\theta | \mathcal{D}))}{H(\pi_1(\theta), \pi_2(\theta))},$$

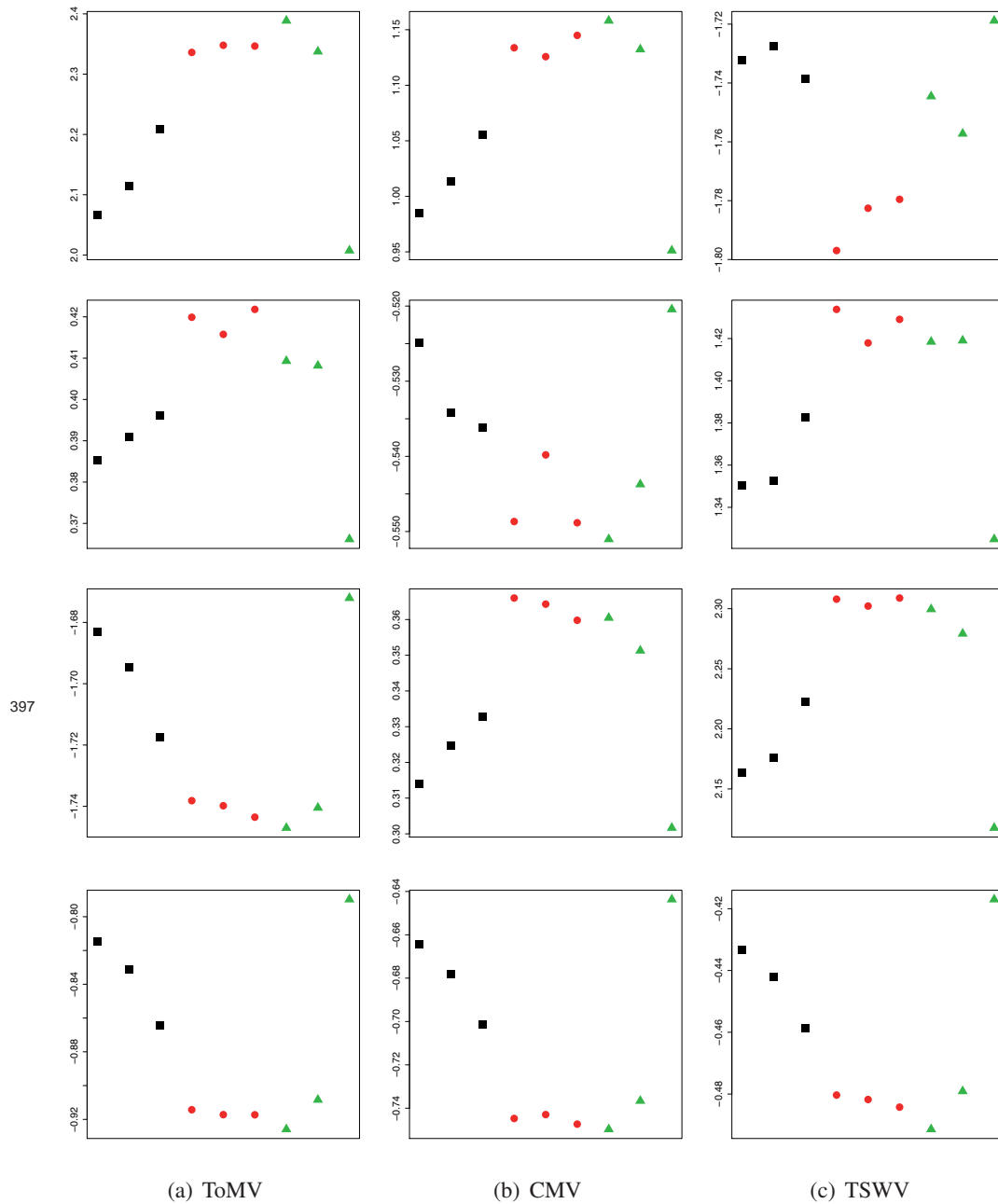


Figure 5: Posterior mean of the regression coefficients associated to plot categories organic (row 1), non organic and greenhouse (row 2), non organic and non greenhouse (row 3), and covariate altitude in logarithmic scale (row 4) for viruses ToMV (column 1), CMV (column 2), and TSWV (column 3) obtained from the full inferential process based on G1, G2 and G3 (black), Un1, Un2 and Un3 (red) and HN1, HN2 and HN3 (green) hyperpriors.

398

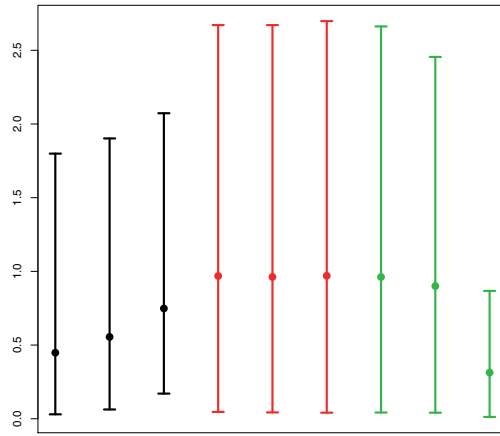


Figure 6: Posterior mean and 95% credible interval for σ_b obtained from hyperpriors Ga1, Ga2, and Ga3 in black, Un1, Un2, and Un3 in red, and HN1, HN2, and HN3 in green.

399 where $\pi_1(\theta | \mathcal{D})$ and $\pi_2(\theta | \mathcal{D})$ are the subsequent posterior distributions from $\pi_1(\theta)$ and
 400 $\pi_2(\theta)$. Note that $S(\pi_1, \pi_2)$ only depends on the Hellinger distance, and consequently,
 401 because of its invariancy to any one-to-one transformations we can parameterize the
 402 prior and posteriors in terms of τ_b or σ_b .

403 As expected, sensitivity values with gamma hyperpriors are very relevant, $S(\text{Ga1}, \text{Ga2})$
 404 $= 0.274$ and $S(\text{Ga1}, \text{Ga3}) = 0.477$, with calibrated values 0.267 and 0.436 respectively.
 405 Thus, considering a Hellinger priors difference such as that reported between the nor-
 406 mal distributions $N(0, 1)$ and $N(1, 1)$, their corresponding Hellinger posteriors difference
 407 should be understood as equal to that generated between the pair $N(0, 1)$ and $N(0.267, 1)$
 408 in the case of hyperpriors Ga1 and Ga2, $N(0, 1)$ and $N(0.436, 1)$ in the case of Ga1 and
 409 Ga3 (see Appendix 2 for more details of calibration). In contrast, sensitivity values asso-
 410 ciated to uniform hyperpriors are near zero, $S(\text{Un1}, \text{Un2}) = 0.017$, $S(\text{Un1}, \text{Un3}) = 0.010$,
 411 with calibrated values 0.017 and 0.010, despite the Hellinger distance between their
 412 corresponding priors being identical in gamma choices. In the case of the half-normal
 413 hyperpriors, the sensitivity associated to HN1 and HN2 is small (0.071 and calibrated

414 value 0.069) but relevant when comparing HN1 and HN3 ($S(\text{HN1}, \text{HN3}) = 0.588$ and
415 calibrated value 0.576).

416 **4.4. Sensitivity of the risk of plot infection**

417 The risk of plot infection was considered the most appropriate measure to describe re-
418 sults in Section 3 due to its great relevance in agronomic studies. In this sense, the anal-
419 ysis of the variability of the estimates from different modelling prior scenarios could be
420 an important issue, mainly as a measure of confidence and reliability. As it was defined
421 in (4), its posterior estimation will depend on the covariates, regression coefficients and
422 random effects, which show different patterns regarding sensitivity. We carried out a
423 sensitivity analysis for that on a similar basis as that for Section 3: the posterior distribu-
424 tion of the risk infection was calculated for a generic plot situated at altitude 76 meters
425 (the sample median) for each virus and management conditions within each hyperprior
426 scenario.

427 Table 3 shows the calibration of the Hellinger distance between the posterior distri-
428 bution of the risk of plot infection for each management condition and virus. Similarly
429 to the particular behaviour of the regression coefficients, the estimation of the risk of
430 plot infection seems to be weakly influenced by the different hyperprior assumptions. In
431 any case, the discrepancies observed between all the comparisons were not greater than
432 the difference between the normal distribution $N(0, 1)$ and $N(0.583, 1)$, which reveals
433 that Hellinger values are in general close to zero. It is worth noting that the Hellinger
434 distance between normal distributions $N(0, 1)$ and $N(1, 1)$ is 0.343 (see again Table 4 in
435 Appendix 2). In a similar manner, the uniform distributions had the smallest discrepan-
436 cies together with half-normal distributions HN1 and HN2. However, as we expected
437 inferences from HN3 exhibited the greatest discrepancies. Gamma hyperpriors showed
438 substantial discrepancies, above all between Ga1 and Ga3, although these differences
439 did not exceed those obtained from hyperprior HN3. Thus, these outcomes seem to in-

440 dicte that the particular choice of a hyperprior distribution influences the estimation of
 441 the risk infection weakly but in a major extent that in the case of the estimates of the
 442 regression coefficients.

Table 3: Calibration of the Hellinger distance between the posterior marginal distribution of
 443 the risk infection computed from hyperprior distributions *Ga1* and *Ga2*, *Ga1* and *Ga3*, *Un1* and
Un2, *Un1* and *Un3*, *HN1* and *HN2*, and *HN1* and *HN3*.

Virus	Management	(Ga1,Ga2)	(Ga1,Ga3)	(Un1,Un2)	(Un1,Un3)	(HN1,HN2)	(HN1,HN3)
ToMV	Organic	0.087	0.234	0.011	0.014	0.041	0.583
	Non-organic, greenhouse	0.051	0.139	0.011	0.011	0.029	0.355
	Non-organic, no greenhouse	0.041	0.100	0.015	0.016	0.031	0.268
444 CMV	Organic	0.079	0.213	0.015	0.014	0.041	0.536
	Non-organic, greenhouse	0.039	0.107	0.012	0.010	0.028	0.285
	Non-organic, no greenhouse	0.053	0.142	0.009	0.012	0.028	0.369
TSWV	Organic	0.049	0.128	0.026	0.025	0.037	0.323
	Non-organic, greenhouse	0.040	0.103	0.014	0.009	0.029	0.280
	Non-organic, no greenhouse	0.053	0.142	0.013	0.011	0.030	0.380

445 There are not so many discrepancies among the posterior means of the risk of a
 446 plot infection from the different hyperprior scenarios but there are many in the posterior
 447 variabilities (see Table 4). We accounted for variability in terms of standard deviation be-
 448 cause it is a measure which describes the grade of uncertainty of the quantity of interest
 449 but mainly due to its direct agronomic interpretation. A great similarity in the posterior
 450 standard deviation values is repeatedly appreciated in results derived from *Un1*, *Un2*,
 451 *Un3*, *HN2* and *HN2* scenarios. The *HN3* value was the most different. However, esti-
 452 mates corresponding to *Ga1*, *Ga2* and *Ga3* vary the most, especially in the case of *Ga1*.

453

Table 4: Posterior standard deviation of the risk of a plot infection from the full inferential
 454 process based on *Ga1*, *Ga2*, *Ga3*, *Un1*, *Un2*, *Un3*, *HN1*, *HN2* and *HN3* hyperpriors.

Virus	Management	Ga1	Ga2	Ga3	Un1	Un2	Un3	HN1	HN2	HN3
ToMV	Organic	0.136	0.146	0.161	0.184	0.184	0.184	0.183	0.178	0.118
	Non-organic, greenhouse	0.217	0.224	0.235	0.252	0.252	0.253	0.251	0.248	0.206
	Non-organic, no greenhouse	0.118	0.123	0.131	0.147	0.147	0.147	0.147	0.142	0.109
455 CMV	Organic	0.119	0.127	0.140	0.161	0.161	0.162	0.161	0.156	0.102
	Non-organic, greenhouse	0.161	0.166	0.175	0.190	0.190	0.190	0.189	0.186	0.151
	Non-organic, no greenhouse	0.179	0.186	0.198	0.216	0.216	0.216	0.215	0.211	0.166
TSWV	Organic	0.066	0.071	0.078	0.092	0.093	0.093	0.092	0.088	0.057
	Non-organic, greenhouse	0.172	0.178	0.187	0.203	0.202	0.202	0.201	0.198	0.162
	Non-organic, no greenhouse	0.185	0.192	0.204	0.223	0.223	0.224	0.222	0.218	0.172

456 In this sense, the posterior standard deviation for risk of a plot infection exhibits a con-
 457 siderable sensitivity to hyperparameter specification. For instance, the risk of a ToMV
 458 infection of a generic plot in an organic management system was estimated from 0.028
 459 to 0.553 with 95% probability according to Ga1 scenario, but the subsequent interval in
 460 the Un1 scenario was [0.008,0.734].

461 5. Discussion

462 In this paper we have proposed a Bayesian correlated model (GLMM) to study and
 463 compare the risk of several virus infections in tomato and pepper plots under different
 464 agroecosystem conditions. First, we estimated several models, maintaining model spec-
 465 ification but varying prior scenario default in accordance with different hyperprior distri-
 466 butions for the random effects scale parameter. Next, we conducted a sensitivity analysis
 467 to select the most stable model, in which effects of management conditions, altitude and
 468 random individual effects were assessed by estimating different derived quantities con-
 469 sidered to be agronomically relevant.

470 Regarding the model covariates effect, the risk of plot infection was the quantity
 471 chosen to analyse agronomic outcomes. The risk of plot infection was estimated in the
 472 framework of mixed infections (with more than one virus) as well as in single infections

473 (with only one virus). All the quantities applied for a “generic” plot of the population of
474 each one of the agroecosystems considered. In the case of single infections, risk differ-
475 ence was also used to quantify differences among agroecosystems. Individual random
476 effects were evaluated by assessing differences in the estimation of the risk of infection
477 among plots managed under similar agroecosystem conditions. This enables the evalua-
478 tion of the contribution of the common and of the individual elements in the model, and
479 therefore the explanatory capacity of covariates.

480 In the case of mixed infections, organic agroecosystems exhibited lower prevalence
481 for a three viruses joint infection. Non organic plots, independently of the presence of a
482 greenhouse structure, showed a similar behaviour. Single infections were generally less
483 prevalent or similar in organic systems than in conventional (non-organic with and with-
484 out greenhouse), while TSWV and CMV infections were less prevalent under organic
485 management; ToMV infection showed a slightly different behaviour pattern possibly
486 as a consequence of the way it is transmitted (mechanical transmission). Altitude ef-
487 fect was clearly negative in all viruses but displayed considerable variability among the
488 three viruses. Random effects behaviour was very regular in individuals belonging to
489 non-organic with greenhouse and non-organic with no greenhouse considering that in-
490 dividual effects did not generate great differences among plots’ risk infection estimates.
491 Organic individuals exhibited more variable results in this aspect, but in general we can
492 assume that all the fixed effects included in the model have a good explanatory capacity.

493 Sensitivity analysis was based on the methodology developed by [Roos and Held](#)
494 [\(2011\)](#) and [Roos et al. \(2015\)](#). Hellinger distance and sensitivity measure, together with
495 their corresponding calibration, allowed us to assess discrepancies in the estimation of
496 the fixed effects (regression coefficients), the random effects standard deviation σ_b as
497 well as the “generic” risk of infection among the prior scenarios tested. The evaluation
498 of the posterior mean of the regression coefficients, the graphical characterization of the

499 marginal posterior distribution of σ_b and the assessment of the standard deviation of the
 500 posterior distribution of the risk of plot infection among the several modelling scenarios
 501 completed the analysis. The outcomes obtained exhibited an insensitive behaviour of
 502 the fixed effects to hyperprior alterations with Hellinger values very close to zero and
 503 to each other. Only visual analysis of posterior means enabled us to detect a certain
 504 instability among inferences obtained from models under gamma hyperdistributions.

505 The estimation of σ_b showed a highly sensitive behaviour: gamma hyperpriors re-
 506 peatedly exhibited the most relevant differences showing the greatest sensitivity values
 507 and the most divergent posterior distributions. In the case of risk infection estimation, in
 508 spite of all the Hellinger distances were around zero, gamma hyperdistributions showed
 509 interesting differences in terms of the standard deviation of the posterior distribution of
 510 the risk of plot infection. We therefore agree with [Browne and Draper \(2006\)](#), [Roos et al. \(2015\)](#),
 511 [Roos and Held \(2011\)](#), [Gelman \(2006\)](#), and [Lunn et al. \(2009\)](#) that gamma hy-
 512 perpriors in hierarchical models lack robustness and a sensitivity analysis must be carried
 513 out in the Bayesian hierarchical framework to assess reliability of the performance. Fur-
 514 thermore, we also conclude that the “noninformative” nature of a hyperprior does not
 515 guarantee its impartiality in the inference process.

516 **Appendix 1. The Hellinger distance**

The Hellinger distance ([Le Cam, 2012](#)) is a symmetric and invariant to any one-to-one transformation measure of discrepancy between two probability distributions, f and g , defined as follows

$$H(f, g) = \sqrt{\frac{1}{2} \int_{-\infty}^{+\infty} (\sqrt{f(u)} - \sqrt{g(u)})^2 du},$$

517 where $0 \leq H(f, g) \leq 1$, 0 represents no divergence, and 1 full divergence.

518 The Hellinger distances between two gamma, uniform and half-truncated distribu-

519 tions are

- for gamma densities $\text{Ga}(\alpha_1, \beta_1)$ and $\text{Ga}(\alpha_2, \beta_2)$

$$H^2(\text{Ga}(\alpha_1, \beta_1), \text{Ga}(\alpha_2, \beta_2)) = 1 - \Gamma\left(\frac{\alpha_1 + \alpha_2}{2}\right) \sqrt{\frac{\beta_1^{\alpha_1} \beta_2^{\alpha_2}}{\Gamma(\alpha_1)\Gamma(\alpha_2)\left(\frac{\beta_1 + \beta_2}{2}\right)^{\alpha_1 + \alpha_2}}}$$

- for uniform densities $\text{Un}(0, \eta_1)$ and $\text{Un}(0, \eta_2)$, with $\eta_1 \leq \eta_2$

$$H^2(\text{Un}(0, \eta_1), \text{Un}(0, \eta_2)) = 1 - \left(\frac{\eta_1}{\sqrt{\eta_1 \eta_2}}\right)$$

- for half-normal densities $\text{HN}(0, \sigma_1^2)$ and $\text{HN}(0, \sigma_2^2)$

$$H^2(\text{HN}(0, \sigma_1), \text{HN}(0, \sigma_2)) = 1 - \frac{\frac{1}{\sigma_1^2} \frac{1}{\sigma_2^2}^{1/4}}{\sqrt{\frac{1}{\frac{\sigma_1^2}{2} + \frac{\sigma_2^2}{2}}}}$$

520 In the case of posterior distributions $\pi_1(\boldsymbol{\theta} | \mathcal{D})$ and $\pi_2(\boldsymbol{\theta} | \mathcal{D})$, the Hellinger distance
521 can be approximated numerically at a finite set of K integration points as follows

$$H^2(\pi_1(\boldsymbol{\theta} | \mathcal{D}), \pi_2(\boldsymbol{\theta} | \mathcal{D})) = \frac{1}{2} \sum_{k=1}^K \left(\sqrt{\pi_1(\boldsymbol{\theta} | \mathcal{D})(k)} - \sqrt{\pi_2(\boldsymbol{\theta} | \mathcal{D})(k)} \right)^2 \Delta_k, \quad (\text{A.1})$$

522 where the weights Δ_k are provided by the trapezoidal rule.

523

524 Appendix 2. Calibration

The Hellinger distance can be calibrated to evaluate the importance of the observed discrepancies by means of a reference parameter. Calibration was undertaken with respect to the normal distribution with variance one. The Hellinger distance between densities

$N(0, 1)$ and $N(\mu, 1)$ is

$$H(N(0, 1), N(\mu, 1)) = \sqrt{1 - \exp(-\mu^2/8)},$$

and consequently

$$\mu = \sqrt{-8 \log(1 - H^2(N(0, 1), N(\mu, 1)))}$$

525 Table A.2.1 shows a range of calibrated values μ with its subsequent Hellinger distance,

526 $H(N(0, 1), N(\mu, 1))$.

527

Table A.2.1: Calibration of the Hellinger distance.

μ	$H(N(0, 1), N(\mu, 1))$
0	0
1	0.343
2	0.627
3	0.822
4	0.930
5	0.978
6	0.994
7	0.999
8	0.999
9	0.999
10	1

528

529 The sensitivity measure introduced previously can also be calibrated. Calibration of

530 the sensitivity value obtained, s , has been obtained following the subsequent equation:

$$C(s, \mu') = \mu(s \times H(N(0, 1), N(\mu', 1))) \quad (\text{A.2})$$

531 Interpretation of calibration can be conditioned by the choice of μ' , so that for a value

532 $\mu' = 1$, the value of s , would be comparable with the Hellinger distance obtained be-

533 tween two normal priors, $N(0, 1)$ and $N(\mu' = 1, 1)$ and the subsequent normal posteriors,

534 $N(0, 1)$ and $N(C(s, \mu' = 1), 1)$. It is important to note that if $s > 1$ then $C(s, \mu') > \mu'$; if
535 $s < 1$ then $C(s, \mu') < \mu'$; and if $s = 1$ then $C(s, \mu') = \mu'$.

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